

Research Statement

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Background

My research passion lies in **Machine Learning** (ML), a subfield of Artificial Intelligence (AI) which studies algorithms that learn from data without being explicitly programmed. I have worked with both Neural Networks (NN) and **Matrix Completion** (MC) models, proving statistical guarantees as well as proposing new algorithmic solutions for problems ranging from Computer Vision (CV) to **Recommender Systems** (RS). Having moved to the field of AI from a background in mathematics, I see a natural connection between the statistical theory of ML models and algorithm design: a starting point in much of my research is **Statistical Learning Theory** (SLT), which broadly concerns the estimation of the number of samples required to train an ML model effectively. In short, I am interested in understanding why ML algorithms work, and in using the insights derived to obtain gains in interpretability and new theoretically motivated algorithms. In addition, statistical guarantees can often help practitioners choose between several architectures for a given problem. In terms of specific classes of ML models, much of both my theoretical and practical research has recently focused on Matrix Completion and Recommender Systems.

Recommender Systems (RS) aim to guide users in a personalized way to items maximizing user satisfaction while providing business value (e.g. increased revenue, engagement) for the recommendation provider. For instance, streaming companies such as Netflix or Douban recommend movies to customers based on previous feedback (clicks, “likes”, etc.), allowing users to discover and watch movies they are more likely to enjoy and which would otherwise have been difficult to single out from the multitude of possibilities. In the simplest case, the recommendation task consists in predicting the user-item ratings based only on the existing observed ratings. This task can be viewed as completing the missing entries of a partially observed matrix, a simple and elegant problem with a surprisingly rich (and yet not quite complete) mathematical theory. In practice, real-world recommender systems rely on much more than the explicit feedback contained in the observed ratings. The implicit feedback implied by the subset of items which each user has chosen to interact with arguably contains just as much information. In addition, in the current paradigm of Web 2.0, users contribute content and interact with each other in various ways in blogs, Twitter, social media websites and other platforms, providing a wealth of heterogeneous information which is relevant to the recommendation task. Incorporating such information into well-principled RS and MC models presents an unparalleled source of opportunities and challenges in both theory and practice.

I also have a strong interest in the theoretical properties of deep neural networks (NN). In general, classic methods struggle to fully explain why such models perform so well even when the number of parameters is much more than the number of samples: it is increasingly clear that underlying structure in the data has as much effect as algorithm

construction on the statistical properties and behavior of deep learning models. For instance, Convolutional Neural Networks (CNN) exhibit especially strong success in image recognition due to the presence of repetitive patterns in the data. Defining and quantifying such effects is especially difficult due to the surprising generality of the phenomenon for many types of ‘natural’ data. The Neural Tangent Kernel (NTK) provides both partial answers to these theoretical questions and huge application potential.

My recent research can be categorized into three interconnected directions: Statistical Learning Theory, Matrix Completion/Recommender Systems, and other Applications (e.g. CV). My most distinctive work usually concerns the study of the **sample complexity of matrix** completion methods. Previously during my PhD, I have also worked on Stochastic Analysis, the study of random processes in continuous time.

Research Areas

On recommender systems, matrix completion and low-rank methods

In classic MC, a typical assumption is that the ground truth matrix has an *approximate low-rank structure*: there is a small (unknown) number of unobserved hidden user and item features that determine the rating via a simple inner product function. This type of low-rank constraint is ubiquitous in ML applications beyond MC and RS.

There are several ways to implicitly induce approximately low-rank solutions. Several classic approaches include convex relaxations such as the Nuclear Norm or the Max norm, which are the most widely studied in the statistics literature. However, popular alternatives such as the Schatten p quasi norm for $p < 1$ can provide solutions with a stricter low-rank structure. Notably, for $p = 2/d$ for some integer d , Schatten p quasi norm regularization is equivalent to the popular *deep matrix factorization* framework of depth d . This observation is relevant not just to matrix completion but also to other areas of machine learning such as deep neural networks, where the implicit rank sparsity inducing effects of depth are being researched intensely. In [ICML'24] we study such effects in the context of deep matrix factorization. Specifically, we prove a sample complexity of $\tilde{O}\left(r^{1-\frac{p}{2}}n^{1+\frac{p}{2}}\right)$ for Schatten p constrained matrix completion. Here n is the size of the matrix and r is a quantity derived from the Schatten constraint which scales like the rank of the ground truth. When $p \rightarrow 1$, we recover the famous rate of $\tilde{O}(r^{1/2}n^{3/4})$ from Shamir and Schalev-Schwarz JMLR'14. When $p \rightarrow 0$, we recover the complexity converges to a much milder $\tilde{O}(rn)$ which aligns with a parameter counting argument: the bounds capture the rank sparsity effect of depth. We also prove a rate of $\tilde{O}(rn)$ for the uniform sampling case and for a weighted Schatten p quasi norm. In the same paper, we also study various more complex models which apply nonlinear functions to latent matrices, demonstrating that the sample complexity contributions of the latent matrices and the nonlinear functions combine additively.

The Inductive Matrix Completion (IMC) model is a generalization of the basic MC model where side information is provided for the users and the items in the form of a set of feature vectors corresponding to each user and to each item. The assumption is that users with similar feature vectors will also exhibit similar rating behaviors. Thus,

this mathematical model represents a first step towards incorporating user information from the web into RS, assuming only that such information has been preprocessed into feature vectors. Interestingly, this similarity assumption coexists in parallel with the low-rank assumption. Until our paper [NeurIPS'21a], the theoretical analysis of MC and IMC relied on nearly distinct approaches, and sample complexity guarantees for IMC did not take the low-rank constraint into account at all.

In our paper [NeurIPS'21a] we have proved several generalization bounds for the IMC model and introduced an improved regularization strategy for IMC. The first contribution is a bound which incorporates both the low-rank constraint and the side information: ignoring logarithmic terms, the sample complexity is $\tilde{O}(d^{3/2}\sqrt{r})$ in (the distribution-free case) where d is the dimension of the side information, and r is the rank of the ground truth matrix. Thus, the bound is non-trivial when the side information approaches the identity, unlike existing IMC bounds in this distribution-free setting. The second contribution is both theoretical and algorithmic: we have introduced a modification of the regularization strategy which counters the effects of non-uniformity. The strategy involves a data-dependent geometric transformation of predictors before the evaluation of the regularization term. Thus, our model relies on the empirical distribution of the observed entries to adapt the behavior of the regularization term. The solution to this modified optimization problem exhibits a sample complexity which is as good as in the uniform sampling case. Although the algorithm is theoretically motivated, it leads to gains in accuracy in the experiments we ran on classic RS datasets such as MovieLens, LastFM and Douban.

In [AAAI'23], we performed a more detailed theoretical analysis of the sample complexity of IMC where the noise in the observations is assumed to be small. So-called 'exact recovery results' show that if the entries of a matrix are observed exactly (from a uniform distribution), there is a high probability of recovering the full ground truth matrix exactly, so long as the number of samples exceeds a given threshold. This is in contrast to 'approximate recovery results' such as those of [NeurIPS'21a] which prove that the error decays at a certain rate (typically $N^{-1/2}$ where N denotes the sample size). In [AAAI'23], we bridge this gap between approximate and exact recovery for IMC by observing and characterizing a threshold phenomenon: the error drops sharply past the exact recovery threshold and continues to decay at the classic $N^{-1/2}$ rate afterwards, with a multiplicative constant proportional to the variance of the noise.

The odd one out selection problem, which consists in identifying the most unusual object out of a small set of (usually three) comparable objects, is currently gaining a lot of attention fields such as cognitive science. In [TNNLS'24], we explore a generalization of such a problem to the recommender systems scenario by identifying movies which are likely to elicit the most distinct ratings out of a group of three movies. Our model incorporates architectural novelties in the modelling of the context vector through multiple use of permutation layers which enforce symmetry of the contextual representation.

[NeurIPS'21b] deals with density estimation under the assumption that the density is approximately low-rank, i.e. the sampling distribution is well approximated by a mixture of processes each of which has independent components. We obtained sample complexity guarantees for a low-rank histogram model with polynomial

dependence on the ambient dimension, whilst traditional guarantees for the standard histogram suffer from the curse of dimensionality. This work is closer to traditional mathematical statistics and not directly related to RSs, but it relies on matrix and tensor decompositions that are commonly used in RS and even other ML applications.

In [TNNLS'21], we introduced a novel matrix completion method for the situation where side information is available in the form of a partition of users and items into distinct categories, or 'communities' according to established terminology. For instance, movies might be categorized by genre (romance, comedy, action, etc.), and items might be divided by gender or nationality. Our model is a sum of several components, including a component for community effects and a component that corresponds to purely low-rank effects independent of the community structure. Thus, our model can disentangle community behavior from individual behavior. Differently from existing works, both community and individual behavior coexist and are combined additively. We also proposed an efficient and scalable optimization implementation based on iterative imputation which takes the 'sparse plus low-rank' structure of the iterates into account. In the spinoff paper [PMLR'21] we extended this paradigm to the situation where the communities must be learned by the model.

In [TNNLS'23], we have explored matrix completion in the presence of a user-level reweighting applied directly to the loss function, and its effects on the nuclear norm regularizer's generalization performance and ability to yield low-rank solutions. As it turns out, a weighted trace norm regularization term analogous to that found in [NeurIPS'21] is required to preserve favorable sample complexity. We also extensively explored the effects of this correction term on both real and synthetic data, demonstrating the superior generalization performance of the model which includes our correction term. In the real data experiments, the reweighting of the loss was applied based on an estimate of the 'reliability' of the user, derived from the level of comprehensiveness in their overall reviews.

In [RecSys'23], a project of my Visiting Research Student, we constructed a joint model with both a low rank matrix completion component and a graph neural network component with dual aims: the matrix completion module estimates the ratings, whilst the graph neural networks component estimates the uncertainty in the ratings. Both modules are trained jointly, with a loss function inspired from the literature on heteroskedastic regression. Extensive experiments demonstrate our method's ability to provide increased performance compared to a single low-rank module and increased interpretability compared to a single graph neural network module. In addition, our model can detect anomalous ratings both in the training set and at test time.

Statistical Learning Theory for neural networks and kernel methods

I have proved generalization bounds for various machine learning models, including CNNs and kernel methods in various scenarios matching popular ML models. I have focused on the so-called "norm-based" approach, which is better suited to the near-infinite parameter spaces ubiquitous in state-of-the-art ML models. In addition, I have paid especially strong attention to applications with extremely large output spaces: extreme multi-class classification, extreme multi-label learning and structured output prediction. The settings are particularly adapted to applications such as handwriting

recognition of words, document tagging and Natural Language Processing (NLP) respectively. In all cases, a central concern is to obtain generalization bounds with a dependency on the number of classes that is as mild as possible.

In [AAAI'21a], we have proved norm-based bounds for CNNs with two main improvements over the state of the art: (1) they take the weight sharing into account, and (2) they have near optimal dependence on the number of classes. Up to logarithmic terms, the bounds do not change much if an identical set of trainable weights is applied to many different areas of an input image. This work was thus the first one to provide statistical guarantees for neural networks which take the translational invariance of CNNs into account in a norm-based context. In addition, in a class-balanced scenario, the dependence on the number of classes is linear (up to log factors) when expressed in terms of sample complexity, which is clearly optimal (as one needs to observe at least one sample from each class in that case). There are plenty of other refined bounds in the paper, including insights on the effect of local Lipschitzness and appropriate batch normalization on generalization performance.

In [AAAI'21b], the multi-class aspect of the above work was extended to the multi-label case, where each input can be associated with an arbitrary number of labels. In [IJCAI'21a], we pushed similar techniques to the extreme, providing bounds with optimal dependence on the dictionary size for structured output prediction for both kernel methods and simple NN architectures. In [NeurIPS'20], we provided model-agnostic generalization bounds for the Stochastic Gradient Descent algorithm.

In [AISTATS'24], we rely on adversarial smoothing to provide some of the first non-vacuous PAC-Bayesian generalization bounds for neural networks in the adversarial setting.

In Computer Vision (CV), interpretability, and other applications

In [WWW'24], we propose a model of web time series such as twitter feeds or YouTube views which posits that external events such as viral trends not only cause short burst of activity, but also alter the underlying dynamics of the consistent audience of the relevant channel. Mathematically, the model is a combination of a three interacting point processes: two Non-homogeneous Poisson Processes and an SFP process. The model is fitted through an EM algorithm, demonstrating compelling results on various datasets extracted from Google Trends and other sources.

In [IJCAI'24] we study interpretable multimodal learning with controlled modality interactions. More specifically, we propose apply an algebraic manipulation to the outer products of each modality's features which ensures that outer products formed from multiple modalities cannot mimic the features of smaller subsets of the same modalities: this allows us to *disentangle the contributions* from each modality or combination thereof whilst preventing the model from always choosing the most inclusive combinations. We experimentally validate the success of the method at isolating relevant modalities or combinations on synthetic datasets, and showcase the results on real life sentiment analysis datasets.

In video tracking, target appearance can vary over time. For instance, a person may be slowly turning, sometimes facing the camera and sometimes having their back to

it. Furthermore, since models must rely on the previous positions of the target (which can only be estimated by the model and are not labeled), errors can propagate and amplify through time. In [AAAI'21c], we proposed a video tracker based on a Siamese architecture that adapts to such situations by constructing an aggregate feature representation based on a representative sample of previous frames. The model also incorporates an estimation of uncertainty which is then used by different model components to improve robustness. In [IJCAI'21b] we investigated various notions of interpretability in NN models for computer vision: for instance, some neurons can be shown to learn concepts corresponding to scenes or objects or colors, or to be scouting for certain specific patterns. The main novelty in our work is that we proposed several regularization strategies that induce greater interpretability during training.

In Stochastic Analysis (PhD)

During my PhD, I proved upper bounds for the densities of low-dimensional projections of high-dimensional Stochastic Differential Equations (SDE) under conditions on the driving vector fields which are analogous to ellipticity or hypoellipticity. The idea is that no matter how complex a system of SDEs is, 'low-dimensional snapshots' of its solution still have 'almost as well-behaved' densities as those of solutions to SDEs directly constructed in the low-dimensional target space. Although the thesis itself is technical due to the great generality of the results, specific systems of SDEs have been used to model both biological neural networks and financial markets.

Selected Publications and Outputs

On Recommender Systems, Matrix Completion and low-rank methods:

[ICML'24] LEDENT, Antoine and ALVES, Rodrigo. Generalization Analysis of Deep Nonlinear Matrix Completion. Proceedings of the 41st International Conference on Machine Learning (ICML), PMLR 235:26290-26360, 2024.

[TNNLS'24] ALVES, Rodrigo; LEDENT, Antoine; and KLOFT, Marius. Context-Aware Representation: Jointly Learning Item Features and Selection From Triplets. IEEE Transactions on Neural Networks and Learning Systems. Published: April 10, 2024. Pages: 1-14. DOI: 10.1109/TNNLS.2023.3288769.

[TNNLS'23] ALVES, Rodrigo; LEDENT, Antoine; and KLOFT, Marius. Uncertainty-Adjusted Recommendation via Matrix Factorization With Weighted Losses. IEEE Transactions of Neural Networks and Learning Systems. Pages: 1-14. DOI: 10.1109/TNNLS.2023.3288769.

[RecSys'23] KASALICKY, Petr; LEDENT, Antoine; and ALVES, Rodrigo. Uncertainty-adjusted Inductive Matrix Completion with Graph Neural Networks. Proceedings of the 17th ACM Conference on Recommender Systems, 1169-1174 (Late Breaking Results).

[AAAI'23] LEDENT, Antoine; ALVES, Rodrigo; LEI, Yunwen; GUERMEUR, Yann; and KLOFT, Marius (2023). Generalization Bounds for Inductive Matrix Completion in Low-Noise Regimes. Proceedings of the AAAI Conference, to appear.

[NeurIPS'21a] LEDENT, Antoine; ALVES, Rodrigo; LEI, Yunwen and KLOFT (2021). Fine-grained generalisation analysis of inductive matrix completion. Advances in Neural Information Processing Systems (NeurIPS) 34, 2021. 25540—25552.

[TNNLS'21] LEDENT, Antoine; ALVES, Rodrigo; and KLOFT, Marius (2021). Orthogonal Inductive Matrix Completion. IEEE Transactions of Neural Networks and Learning Systems. Pages : 1-12, DOI : 10.1109/TNNLS.2021.3106155.

[NeurIPS'21b] VANDERMEULEN, Rob; and LEDENT, Antoine (2021). Beyond Smoothness : Incorporating Low-Rank Analysis into Nonparametric Density Estimation. Advances in Neural Information Processing Systems (NeurIPS) 34, 12180—12193.

[RecSys'21] ALVES, Rodrigo; LEDENT, Antoine; and KLOFT, Marius (2021). Burst-induced Multi-Armed Bandit for Learning Recommendation. Recommender Systems Conference (RecSys) 2021, 292-301. DOI: <https://doi.org/10.1145/3460231.3474250>

[PMLR'21] ALVES, Rodrigo; LEDENT, Antoine; ASSUNÇÃO, Renato; and KLOFT, Marius (2021). An Empirical Study of the Discreteness Prior in Low-Rank Matrix Completion. NeurIPS 2020 Preregistration Workshop. Proceedings of Machine Learning Research (PMLR) 148:111-125, 2021.

On the statistical theory of neural networks and kernel methods:

[AISTATS'24] MUSTAFA, Waleed; LIZNERSKI, Philipp; LEDENT, Antoine; WAGNER, Dennis; WANG, Puyu; and KLOFT, Marius. Non-vacuous Generalization Bounds for Adversarial Risk in Stochastic Neural Networks. Proceedings of The 27th International Conference on Artificial Intelligence and Statistics, Pages: 4528–4536. DOI: 10.48550/arXiv.1703.11008.

[AAAI'21a] LEDENT, Antoine; MUSTAFA, Waleed; LEI, Yunwen; and KLOFT, Marius (2021). Norm-based generalisation bounds for convolutional neural networks, by Proceedings of the AAAI Conference on Artificial Intelligence (AAAI), 35(9), 8279-8287.

[AAAI'21b] Liang WU, Antoine LEDENT, Yunwen LEI and Marius KLOFT (2021). Fine-grained Generalization Analysis of Vector-valued Learning. Proceedings of the AAAI Conference on Artificial Intelligence, 35(12): 10338-10346.

[IJCAI'21a] MUSTAFA, Waleed; LEI, Yunwen; LEDENT, Antoine; and KLOFT, Marius (2021). Fine-grained Analysis of Structured Output Prediction. Proceedings of the Thirtieth International Joint Conference on Artificial Intelligence, IJCAI-21. 2841-2847.

[NeurIPS'20] LEI, Yunwen; LEDENT, Antoine; and KLOFT, Marius (2020). Sharper generalisation bounds for pairwise learning. *Advances in Neural Information Processing Systems (NeurIPS)* 33, 21236–21246.

In Computer Vision (CV), time series analysis and other applications:

[WWW'24] ALVES, Rodrigo; LEDENT, Antoine; ASSUNÇÃO, Renato; VAZ-DE-MELO, Pedro; KLOFT, Marius. Unraveling the Dynamics of Stable and Curious Audiences in Web Systems. *Proceedings of the ACM on Web Conference 2024*, 2464-2475.

[IJCAI'24] VARSHNEYA, Saurabh; LEDENT, Antoine; LIZNERSKI, Philipp; BALINSKY, Andriy; MEHTA, Purvanshi; MUSTAFA, Waleed; KLOFT, Marius. Interpretable Tensor Fusion. *Proceedings of the Thirty-Third International Joint Conference on Artificial Intelligence (IJCAI-24)*.

[AAAI'21c] ZHOU, Lijun; LEDENT, Antoine; HU, Qintao; LIU, Ting; ZHANG, Jianlin; and KLOFT, Marius (2021). Model Uncertainty Guides Visual Object Tracking. *Proceedings of the AAAI Conference on Artificial Intelligence*, 35(4): 3581-3589.

[IJCAI'21b] VARSHNEYA, Saurabh; LEDENT, Antoine; VANDERMEULEN, Rob; LEI, Yunwen; ENDERS Matthias; BORTH Damian; and KLOFT, Marius (2021). Learning Interpretable Concept Groups in CNNs. *Proceedings of the Thirtieth International Joint Conference on Artificial Intelligence, IJCAI-21*, 1061-1067.

In Stochastic Analysis:

[PhD'17] LEDENT, Antoine. Sharper Kusuoka-Stroock type bounds for densities related to low-dimensional projections of high dimensional SDEs. PhD Thesis, University of Luxembourg.